

## Boyle's Law

Describes the relationship between pressure and volume of a gas

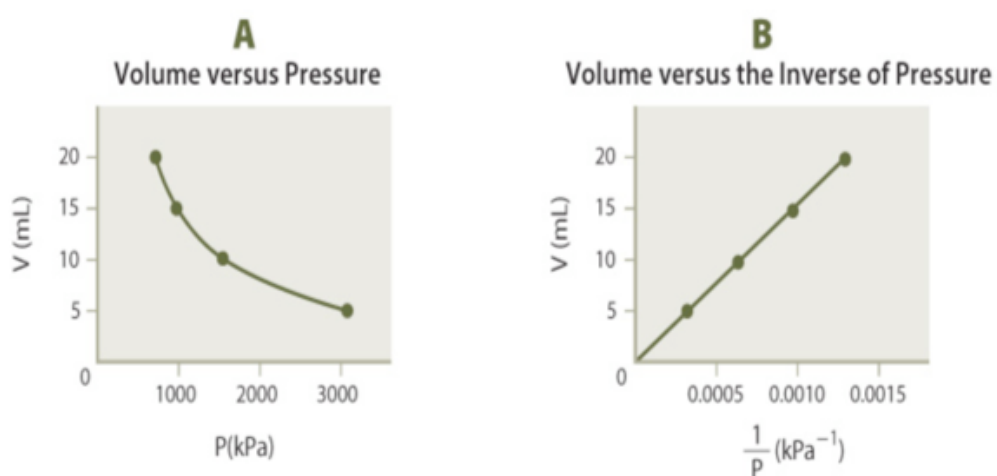
As pressure increases volume decreases

This is called an inverse relationship

$$V \propto 1/P$$

$$V \times P = \text{constant}$$

# Graphs



**Figure 3.11** The graph for volume versus pressure (**A**) shows an inverse relationship. When you plot volume versus the inverse of pressure (**B**), you get a straight line.

## Equation

$$V_1 P_1 = V_2 P_2$$

Applies to constant temperature and constant amount (# of moles) of gas

Units of volume and pressure need to be the same on both sides of the equation

Example #1

A sample of gas has a pressure of 750 torr and a volume of 20.5 mL. What will be the new volume of the gas when the pressure is 800 torr?  $\rightarrow P_2$

$$V_1 \cdot P_1 = \frac{V_2 P_2}{P_2}$$

$$\frac{V_1 P_1}{P_2} = V_2$$

$$\frac{(20.5 \text{ mL}) (750 \text{ torr})}{800 \text{ torr}} = V_2$$

$$19.2 \text{ mL} = V_2$$

$$19.2 \text{ mL} = V_2$$

## Example #2

What will happen to the pressure of a gas if the volume is doubled? (Prove this mathematically)

$$V_1 P_1 = V_2 P_2$$
$$\frac{\cancel{V_1} P_1}{2 \cancel{V_1}} = \frac{\cancel{2V_1} P_2}{\cancel{2V_1}}$$

$$\frac{P_1}{2} = P_2$$

## Example #3

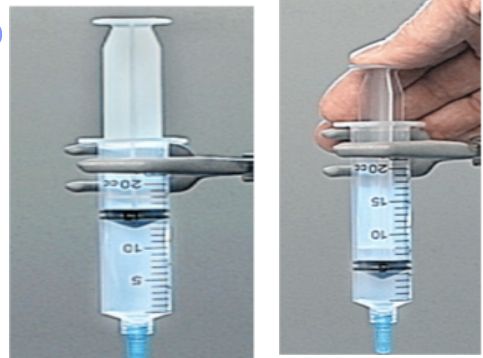
A syringe contains 15 mL of gas at a pressure of 101.3 kPa. If the volume of the syringe is reduced to 5.0 mL, what will be the pressure?

$$\frac{V_1 P_1}{V_2} = \frac{V_2 P_2}{V_2}$$

$$\frac{V_1 P_1}{V_2} = P_2$$

$$\frac{(15 \text{ mL}) (101.3 \text{ kPa})}{(5.0 \text{ mL})}$$

$$= P_2 = 3.0 \times 10^2 \text{ kPa}$$

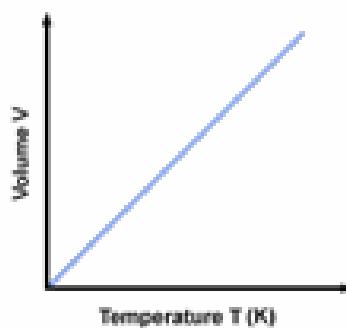


## Charles's Law

The relationship between the volume and Kelvin temperature of a gas is direct

as one increases so does the other one

a graph of volume and temperature of a gas is a straight line



# Formula

This formula can be used when  
pressure and moles of gas are  
constant

T must be in Kelvin



Example 2

What will happen to the volume of a gas if the pressure is tripled? (Prove this mathematically)

Example 3

How hot will a 2.30 L balloon have to get to expand to a volume of 400 L? Assume that the initial temperature of the balloon is 25.0 °C.

Boyle's Law or Charles' Law?

A toy balloon filled with air has an internal pressure of 1.25 atm and a volume of 2.50 L. If I take the balloon to the bottom of the ocean where the pressure is 95 atmospheres, what will the new volume of the balloon be if the temperature remains constant?



Some students believe that teachers are full of hot air. If I inhale 2.2 liters of gas at a temperature of  $18^{\circ}\text{C}$  and it heats to a temperature of  $38^{\circ}\text{C}$  in my lungs, what is the new volume of the gas?

## **Combined Gas Law**

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

Example 1

A gas occupies a volume of 20.0 L at a pressure of 5.00 atm and a temperature of 500 K. What will the volume be if the pressure is raised to 10.0 atm and temperature is changed to 250K

Example 2

A cylinder of compressed nitrogen has a volume of 45.0 L and a pressure of 980 kPa and is kept at a temperature of 30.0°C. The cylinder is heated until it reaches a temperature of 45.0°C. What will the pressure in the cylinder be after it is heated?

### Example 3

If I initially have a gas at a pressure of 500 mm Hg, a volume of 23 liters, and a temperature of 200 K, and then I raise the pressure to 6000 mm Hg and increase the temperature to 300 K, what is the new volume of the gas?

Example 4

I have an unknown volume of gas at a pressure of 0.5 atm and a temperature of 325 K. If I raise the pressure to 1.2 atm, decrease the temperature to 320 K, and measure the final volume to be 48 liters, what was the initial volume of the gas?

